Test II for Calculus II, Math 1502, September 22, 2009

allowed time is 5 mations! For example, otherwise of Print your name	0 minutes. Provide example, if you mean $\sqrt{2}$ deredit cannot be given. ne (not your signature of your TA on EV)	lators and notes of any sorts. The ct answers; not decimal approxilo not write 1.414 Show your are), your section number as ERY PAGE of this test. This

Print Name:

Name of TA:

Section:

Section:

Name of TA:

I: a) Let $\sum_{k=0}^{\infty} a_k x^k$ be a power series of which you only know that it converges at x = c > 0. Does it necessarily follow that

- i) (3 points) The series $\sum_{k=0}^{\infty} k^2 a_k x^k$ converges for x=c?
- ii) (3 points) The series $\sum_{k=0}^{\infty} k^4 a_k x^k$ converges for |x| < c?
- iii) (3 points) The series $\sum_{k=0}^{\infty} \frac{a_k}{k^2} x^k$ converges absolutely at c?
- iv) (3 points) The series $\sum_{k=0}^{\infty} \frac{a_k}{k^2} x^k$ diverges for |x| > c?

You do not have to explain your answer and there is no partial credit.

b) (13 points) Estimate the difference between the limit of the series

$$\sum_{k=0}^{\infty} (-1)^k \frac{k!}{(3k)!}$$

and s_3 , the sum up to k=3. You do not have to simplify your answer.

Section:

Name of TA:

II: (15 points) Find the first three digits after the decimal point of the integral

$$\int_0^1 J_0(x)dx ,$$

where $J_0(x) = \sum_{k=0}^{\infty} (-1)^k \frac{1}{2^k (k!)^2} x^k$. $(J_0(x))$ is called the Bessel function of order 0.) You do not have to simplify your answer.

b) (10 points) Sum the series

$$\sum_{k=1}^{\infty} \frac{k}{2^k}$$

Section:

Name of TA:

III: a) (7 points) Write the power series expansion for

$$\log(1+x) .$$

b) (8 points) Write the power series expansion for

$$\log\left(\frac{1+x}{1-x}\right)$$

c) (10 points) Write the power series expansion of

$$\int_0^x \frac{1}{1+t^4} dt \ .$$

Section:

Name of TA:

IV: a) (10 points) Find the general solution of the differential equation

$$y' + 2xy = x .$$

Check your answer!

b) (15 points) Solve the initial value problem

$$xy' + 4y = x^2$$
, $y(1) = 2$.

Check your answer!