Section:		
Name of TA:		
allowed time is 5 mations! For example, otherwise of Write your name	on minutes. Provide example, if you mean $\sqrt{2}$ caredit cannot be given.  The section is a section of the section of the section is a section of the section is a section of the section of the section is a section of the section is a section of the sec	lators and notes of any sorts. The ct answers; not decimal approxilo not write 1.414 Show your mber as well as the name of test. This is very important.

Test I R for Calculus II, Math 1502 G1-G5 , September 22, 2010

Name:

## Section:

## Name of TA:

- I: (25 points) Consider the function  $e^{-x}$ .
- a) Find the 4-th order Taylor polynomial  $P_4(x)$  for  $e^{-x}$  and the corresponding remainder in Lagrange form.

- b) Using the above result compute an approximate value, call it A, for  $\frac{1}{e}$
- c) Give an estimate on how accurate the value computed in b) approximates  $\frac{1}{e}$ , i.e., give a bound on

$$\left|\frac{1}{e}-A\right|$$
,

using the remainder found in a).

Section:

Name of TA:

II: (25 points) a) Let f(x) be a continuous function on the real line. Compute

 $\lim_{x \to 0} \frac{\int_{-x}^{x} f(y) dy}{2x} .$ 

Compute as well: b)

$$\lim_{x \to 1} \frac{x-1}{x^5-1} \ ,$$

c)

$$\lim_{x \to \infty} \left( 1 + \frac{1}{x} \right)^{4x}$$

**Section:** 

Name of TA:

III: (25 points) Consider the integral

$$\int_0^\infty e^{-x/2} \mathrm{d}x \; ,$$

Write down the definition what mean by 'this integral exists' and then decide whether it indeed exist. Compute its value if it exists.

Similarly for

$$\int_{-\infty}^{\infty} \frac{1}{x^2} \mathrm{d}x$$

Using the comparison principle decide which of the two integrals below exist. State clearly if you use an upper bound or a lower bound in the comparison. You do not have to compute any of the integrals.

b)

$$\int_{1}^{\infty} \frac{1}{\sqrt{1+x^3}} \mathrm{d}x$$

c) 
$$\int_{1}^{\infty} \frac{1}{(1+x^{5})^{1/6}} dx$$

Section:

Name of TA:

IV: (25 points) Which of the following series is convergent or divergent. If it is convergent, sum it.

a)

$$\sum_{k=0}^{\infty} \left(1 + \frac{1}{k}\right)^{-k} .$$

b) 
$$\sum_{k=0}^{\infty} \frac{\sqrt{k+2} - \sqrt{k+1}}{\sqrt{k+1}\sqrt{k+2}} .$$

c) The following series converges

$$L = \sum_{k=1}^{\infty} \frac{9}{10^k}$$

Find L. Moreover, find the smallest n so that  $0 < L - s_n < 10^{-10}$ . Here  $s_n$  is the n-th partial sum.