

NAME:

QUIZ 5 FOR MATH 2551 F1-F4, OCTOBER 3, 2018

This quiz should be taken without any notes and calculators. Time: 20 minutes. Show your work, otherwise credit cannot be given.

Problem 1: (3 points) Find the equation for the plane tangent to the surface $x^2 + y^2 + z^2 = 3$ at the point $(1, 1, 1)$.

Set $f(x, y, z) = x^2 + y^2 + z^2$. At the point $(1, 1, 1)$

$$\nabla f = \langle 2, 2, 2 \rangle.$$

Tangent plane

$$2(x - 1) + 2(y - 1) + 2(z - 1) = 0 .$$

Problem 2: (4 points) Find the the parametric equations for the line tangent to the curve of intersection of the surfaces $xyz = 1$ and $x^2 + 2y^2 + 3z^2 = 6$ at the point $(1, 1, 1)$.

Set $f(x, y, z) = xyz$ and $g(x, y, z) = x^2 + 2y^2 + 3z^2$ then then at the point $(1, 1, 1)$,

$$\nabla f = \langle 1, 1, 1 \rangle , \quad \nabla g = \langle 2, 4, 6 \rangle$$

Direction of line

$$\langle 1, 1, 1 \rangle \times \langle 2, 4, 6 \rangle = \langle 2, -4, 2 \rangle$$

Point on the line $(1, 1, 1)$ so

$$x = 1 + 2t , y = 1 - 4t , z = 1 + 2t$$

Note that the parametrization is not unique, e.g.,

$$x = 1 + t , y = 1 - 2t , z = 1 + 2t$$

would be fine too.

Problem 3: (3 points) Find the linearization $L(x, y)$ of the function $f(x, y) = x^2 + y^2 + 1$ at the point $(1, 1)$. The partials at the point $(1, 1)$ are

$$f_x(1, 1) = 2, \quad f_y(1, 1) = 2$$

and hence the linearization is given by

$$L(x, y) = f(1, 1) + f_x(1, 1)(x - 1) + f_y(1, 1)(y - 1) = 3 + 2(x - 1) + 2(y - 1) .$$